



AN INTRODUCTION TO DEEP LEARNING ON GRAPHS AND CURRENT DEVELOPMENTS

Pedro H.C. Avelar Luis C. Lamb

September 2019

1. Introduction to Graph-Based Learning
2. Graph-based Learning for Superpixel Images
3. Learning on Graphs for Continuous Domains
4. Side Projects
 - Measuring Academic Engagement with Ethics in the Area of AI
 - Second Language Acquisition Modelling with Attentional Models and Half-Life Regression
5. Not Covered Here

Introduction to Graph-Based Learning

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1

INTRODUCTION TO GRAPH-BASED LEARNING

THE GRAPH NEURAL NETWORK MODEL

AN INTRODUCTION TO DEEP
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Main Ideas:

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2. Propagate information until it converges

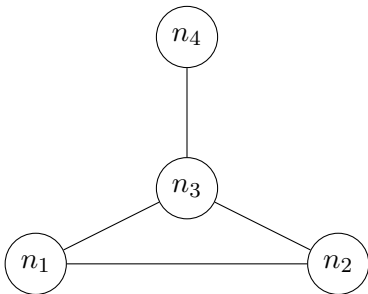
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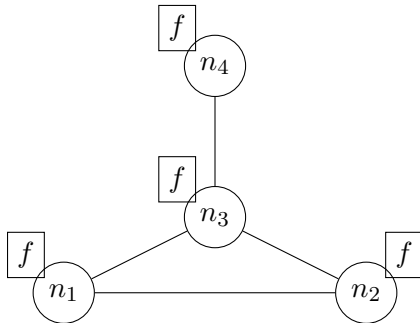
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2. Propagate information until it converges
3. Readout desired information through another neural module

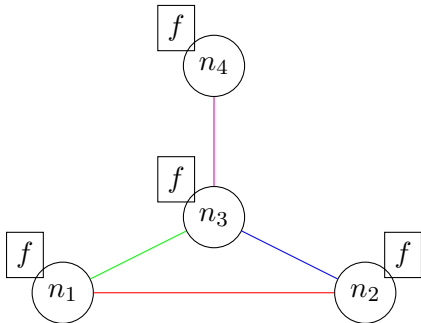
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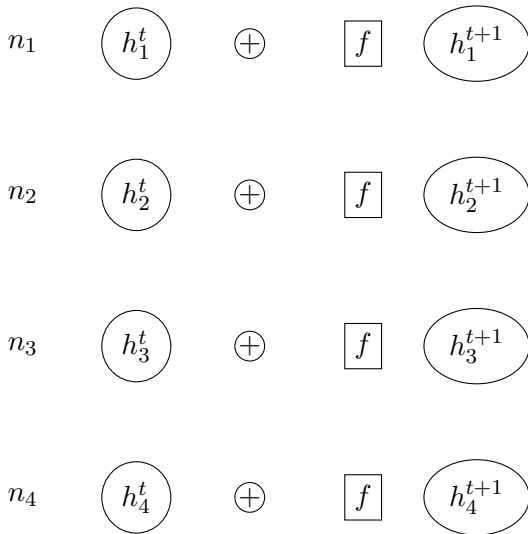
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2. Propagate information until it converges
3. Readout desired information through another neural module
4. [Scarselli et al., 2009] One could adapt this to work with different “kinds” of nodes (i.e. the edge and graph nodes in [Battaglia et al., 2018])

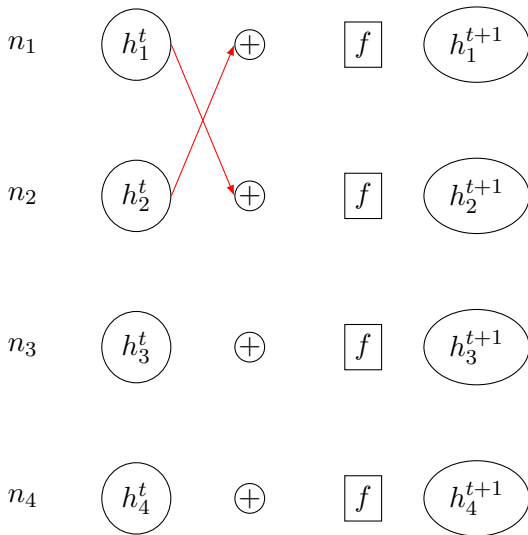
THE GRAPH NEURAL NETWORK MODEL: A GRAPH

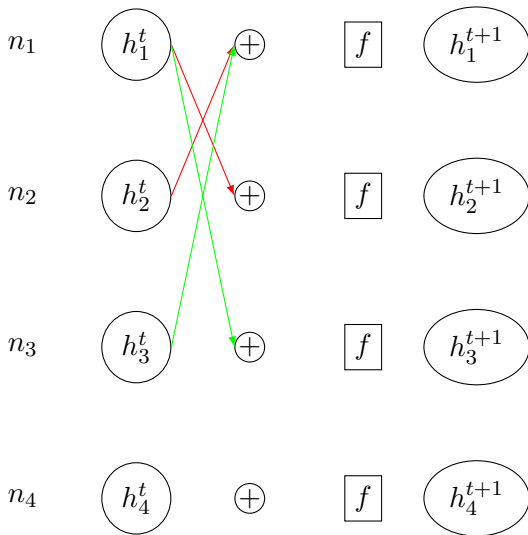


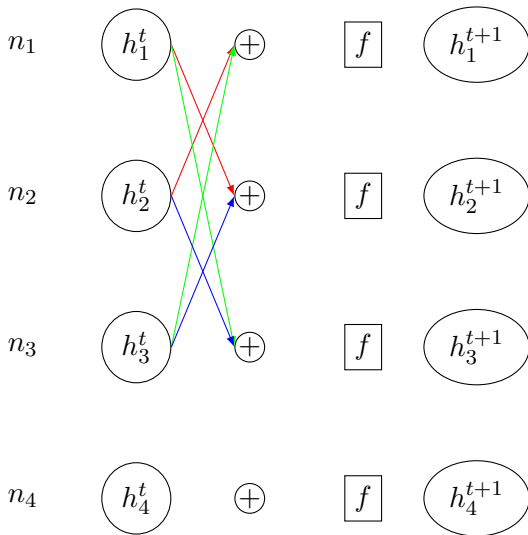


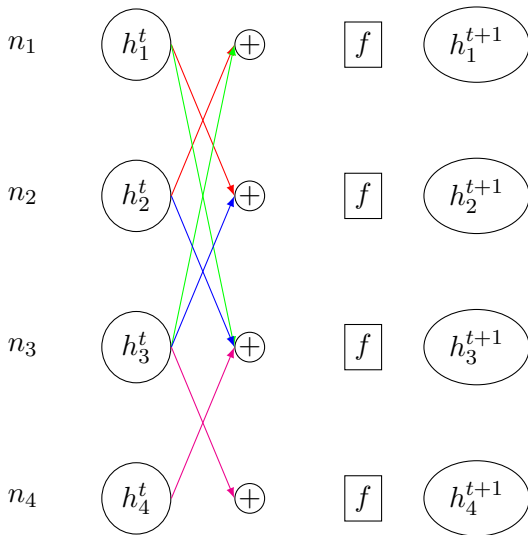


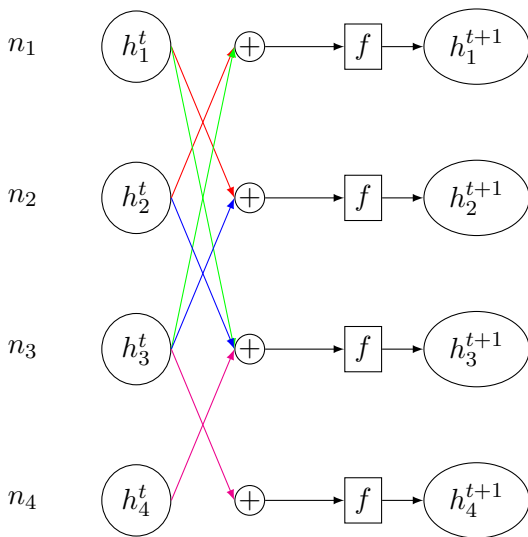
THE GRAPH NEURAL NETWORK MODEL:
ONE PROPAGATION LAYER

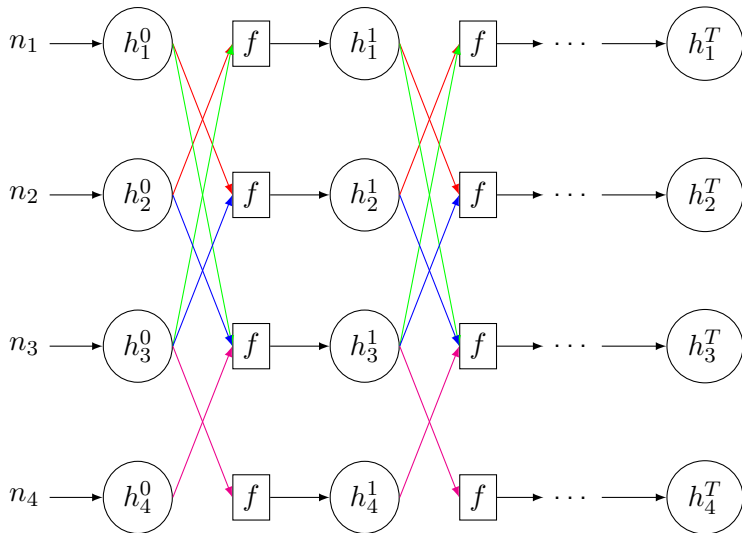
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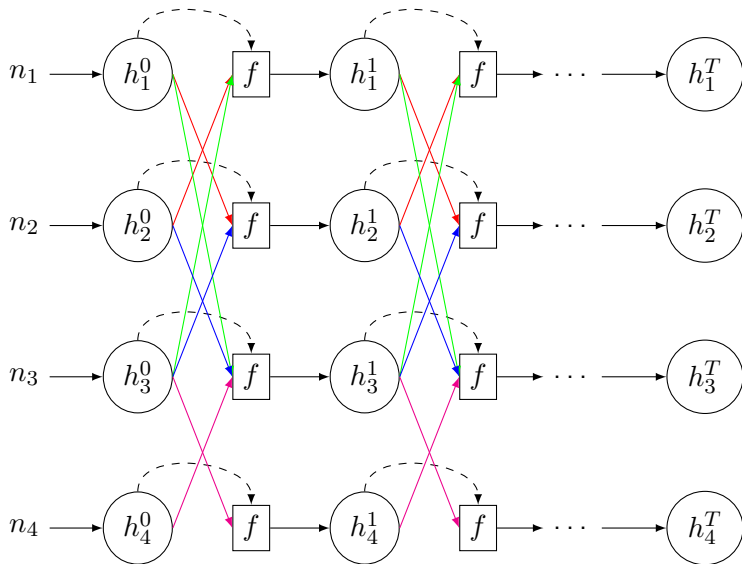
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THE GRAPH NEURAL NETWORK MODEL:
UNROLLING IN TIME

THE GRAPH NEURAL NETWORK MODEL:
RECURRENT CONNECTIONS

With sum-aggregation, it is easy to organise the propagation as matrix multiplication. Given an adjacency matrix \mathbf{M} with shape (n, n) , the learned function f , and the current node “state” \mathbf{h}^t with shape (n, d) , we have:

$$\mathbf{h}^{t+1} = f(\mathbf{M} \times \mathbf{h}^t)$$

Which translates, on a node-to-node basis as:

$$\mathbf{h}_n^{t+1} = f\left(\sum_{j \in \mathcal{N}(n)} \mathbf{h}_j^t\right)$$

With $\mathcal{N}(n)$ being the neighbourhood of node n .

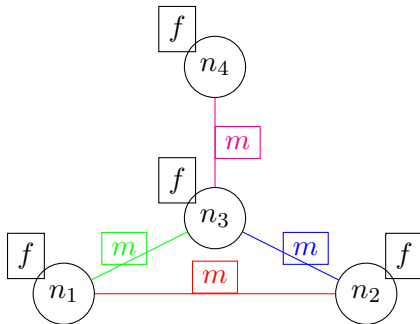
Same principles as [Gori et al., 2005, Scarselli et al., 2009]:

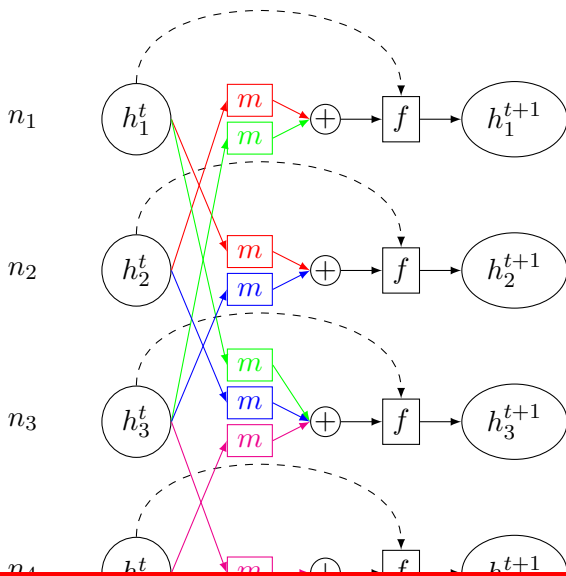
Same principles as [Gori et al., 2005, Scarselli et al., 2009]:

- A separate “messaging” function added between communicating nodes.

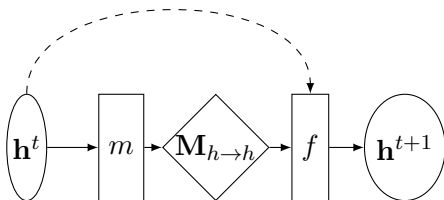
Same principles as [Gori et al., 2005, Scarselli et al., 2009]:

- A separate “messaging” function added between communicating nodes.
- “Messages” propagated for a given number of iterations instead





We'll use the following graphical representation for simplifying the MPNN blocks, ellipses are state tensors, rectangles are learned functions, diamonds represent matrix multiplication (or any other type of neighbourhood aggregation), circles (not present) are pointwise operations, and if two arrows join at a point their tensors are most likely concatenated for every tuple of node:



- Messaging functions often take more than just the source's embedding.
- Neighbourhood aggregation can be made in many ways:
 - Sum-aggregation [Gori et al., 2005, Scarselli et al., 2009, Gilmer et al., 2017, Selsam et al., 2018, Xu et al., 2019]
 - Average-aggregation [Kipf and Welling, 2017]
 - Attentional sum-aggregation [Velickovic et al., 2018]
 - Product-aggregation
 - Or any other order-invariant function
- Readout functions can be really diverse, using only specific nodes, all nodes of a kind/type, pairs of nodes, etc...
- Batching of different input graphs (done as a block-diagonal matrix)

Independently, generalisations of convolutions to graph-domains, such as [Kipf and Welling, 2017], led to an architecture similar to [Scarselli et al., 2009], only with no recurrent connection, untied weights, and average-aggregation instead of sum-aggregation.

[Battaglia et al., 2018] suggests the generalisation of the concept of graph neural networks to models other than neural networks, builds upon this idea of inductive bias and argues for three specific kinds/types of nodes: Vertex, Edge and Graph-level nodes.

We can:

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- Assemble neural modules in the configuration of the input graphs and propagate information through neighbours.
- Work with different “kinds”/types of nodes by training different “update” and “message” functions, working on different sets of embeddings, and different adjacency matrices (we’ll see examples soon).
- Read out the embeddings at the last layer and use them to provide an answer to the problem at hand.

Graph-based Learning for Superpixel Images

2

- Images have superpixel representations

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- These representations can be seen as a graph of superpixels

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- These representations can be seen as a graph of superpixels
- Use graph-based methods to work with this data

2

GRAPH-BASED LEARNING FOR SUPERPIXEL IMAGES

SUPERPIXEL GRAPH

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AND CURRENT
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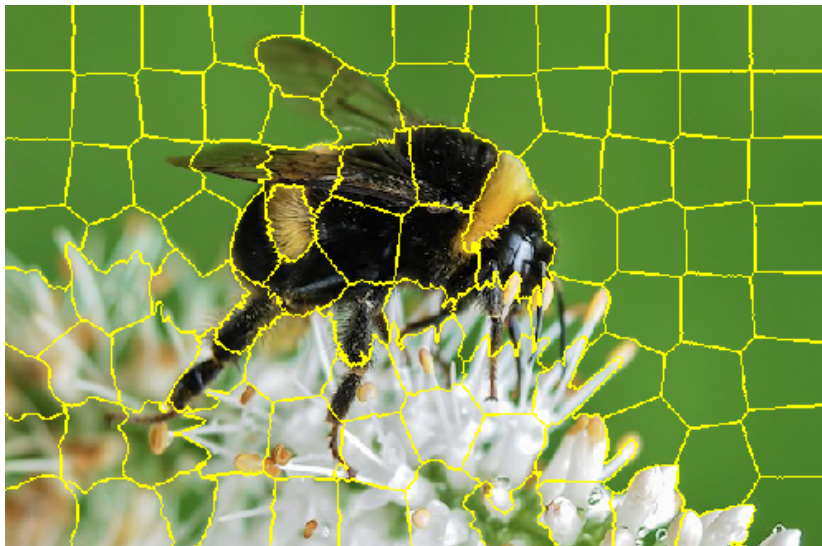


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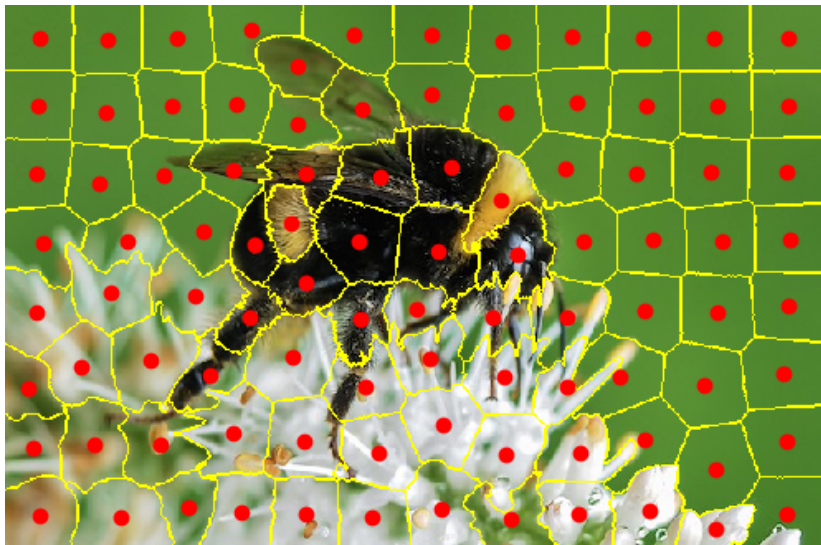


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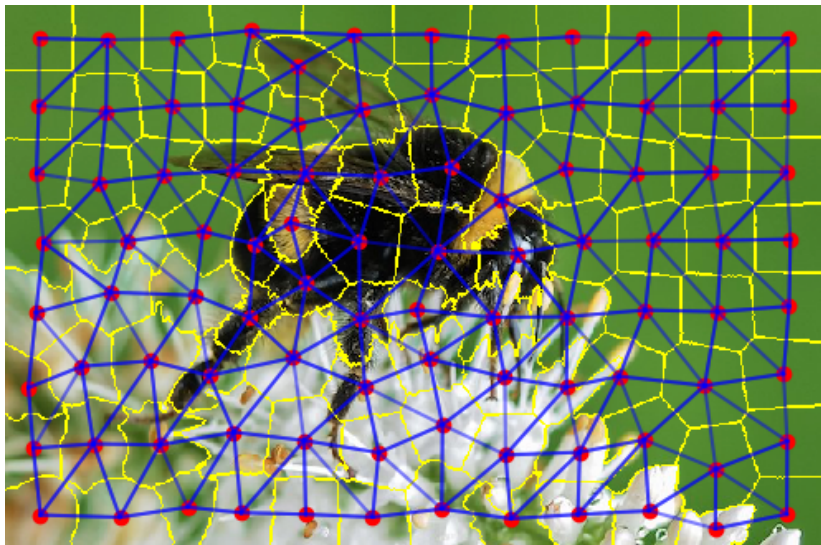


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GRAPH-BASED LEARNING FOR SUPERPIXEL IMAGES

SUPERPIXEL GRAPH

AN INTRODUCTION TO DEEP
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- Color mean/std/Gram matrix (variance matrix)

2

- Color mean/std/Gram matrix (variance matrix)
- Position mean/std/Gram matrix (variance matrix)

2

- Color mean/std/Gram matrix (variance matrix)
- Position mean/std/Gram matrix (variance matrix)
- Superpixel Compactness

2

GRAPH-BASED LEARNING FOR SUPERPIXEL IMAGES

SANITY CHECKING – MNIST

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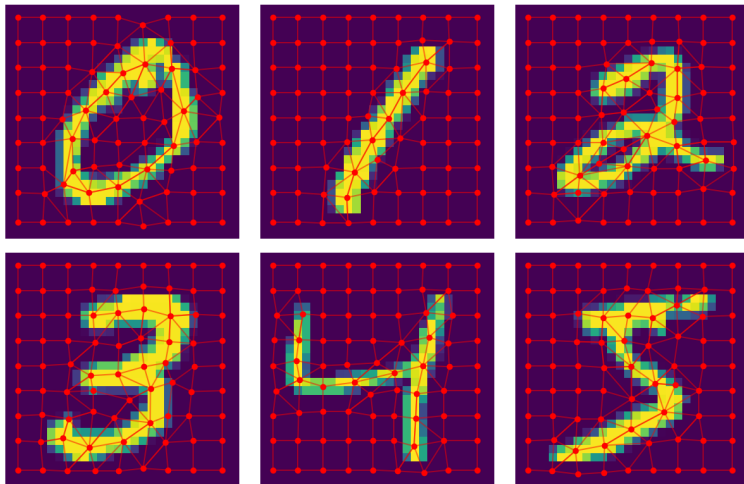


2

GRAPH-BASED LEARNING FOR SUPERPIXEL IMAGES

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2

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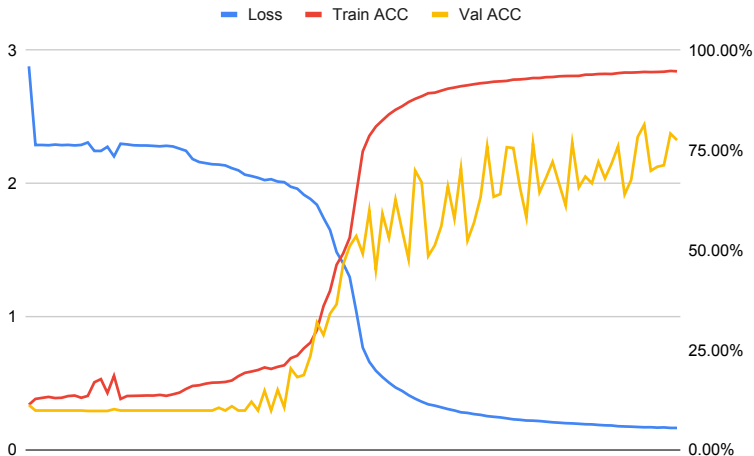
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- An MLP with 2 layers

2

PRELIMINARY RESULTS



Profiling results give us out that performing online segmentation to transform to graphs is too slow:

Code	Time Relative to Batch
Gen Graphs from Images	55.91%
Batching Graphs	18.59%
To Pytorch/GPU	23.21%
GAT	1.03%
Metrics	0.05%
Backprop	1.21%

2

- Generate graphs offline

2

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- Other datasets: Pascal VOC, CoCo (segmentation), Transfer to Spherical Images

2

GRAPH-BASED LEARNING FOR SUPERPIXEL IMAGES

SUGGESTIONS?

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Suggestions?

Learning on Graphs for Continuous Domains

3

- Neural Networks can be put as residual blocks

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- Residual blocks can be interpreted as discrete derivatives
- We can integrate residual blocks to give them continuity
- Why not do this with graphs?

3

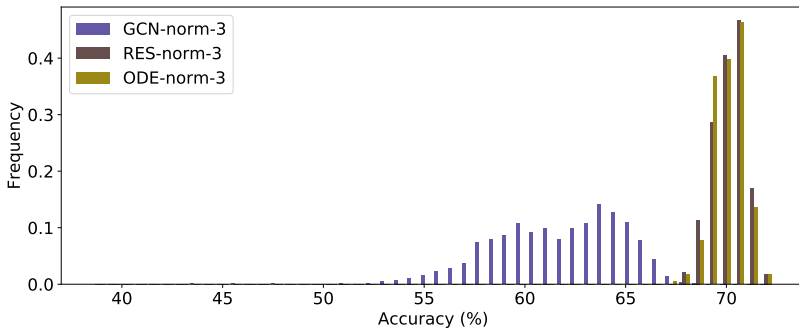
- First tests done with traditional GCN [Kipf and Welling, 2017]

3

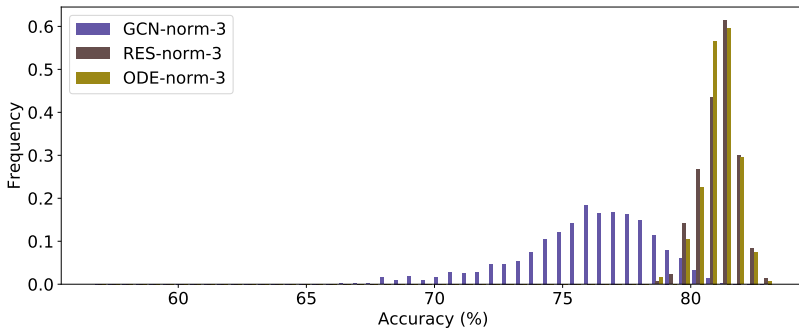
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- Tests performed on traditional node classification datasets:
 - Citeseer
 - Cora
 - Pubmed

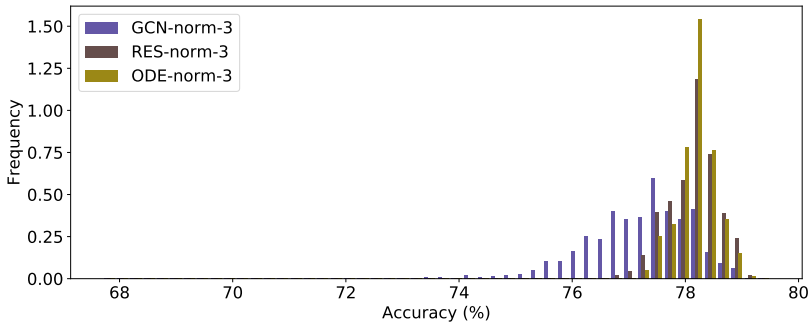
3



3



3



3

LEARNING ON GRAPHS FOR CONTINUOUS DOMAINS PHYSICS

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Working under way to extend this to physics models such as n-body orbits, ball collisions and string/spring physics

3

LEARNING ON GRAPHS FOR CONTINUOUS DOMAINS

SUGGESTIONS?

AN INTRODUCTION TO DEEP
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Suggestions?

Side Projects

4

SIDE PROJECTS

MEASURING ACADEMIC ENGAGEMENT WITH ETHICS IN THE AREA OF AI

MAIN IDEAS

AN INTRODUCTION TO DEEP LEARNING ON GRAPHS AND CURRENT DEVELOPMENTS

- Computing ethics keywords from arxiv paper abstracts from Human-AI field

4

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SIDE PROJECTS

SECOND LANGUAGE ACQUISITION MODELLING WITH
ATTENTIONAL MODELS AND HALF-LIFE REGRESSION

MAIN IDEAS

AN INTRODUCTION TO DEEP
LEARNING ON GRAPHS
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- Using HLR and attention to predict errors learners may do

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- Using HLR and attention to predict errors learners may do
- HLR will model forgetting

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5

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- Differential Gradient (TBD – Planning to present it at Khipu)
- BRHIM (Waiting for data)

 Battaglia, P. W., Hamrick, J. B., Bapst, V., Sanchez-Gonzalez, A., Zambaldi, V. F., Malinowski, M., Tacchetti, M., Raposo, D., Santoro, A., Faulkner, R., Gülçehre, Ç., Song, F., Ballard, A. J., Gilmer, J., Dahl, G. E., Vaswani, A., Allen, K., Nash, C., Langston, V., Dyer, C., Heess, N., Wierstra, D., Kohli, P., Botvinick, M., Vinyals, O., Li, Y., and Pascanu, R. (2018). Relational inductive biases, deep learning, and graph networks. *CoRR*, abs/1806.01261.



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In Precup, D. and Teh, Y. W., editors, *Proceedings of the 34th International Conference on Machine Learning, ICML 2017, Sydney, NSW, Australia, 6-11 August 2017*, volume 70 of *Proceedings of Machine Learning Research*, pages 1263–1272. PMLR.



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Scarselli, F., Gori, M., Tsoi, A. C., Hagenbuchner, M., and Monfardini, G. (2009).

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